

Prof. Dr. Alfred Toth

## Strukturen von Sandwichthematizationen

1. Sandwichthematizationen, die im Teilsystem der 10 semiotischen Dualsysteme nicht auftauchen, wurden erstmals in Toth (2007, S. 176 ff.) beschrieben. Indessen kann man die einzige Realitätsthematik mit triadischer Realität im 10er-System, die mit ihr dualidentische sog. eigenreale Zeichenklasse (vgl. Bense 1992) als Spezialfall von Sandwichthematizationen mit paarweise differenten semiotischen Werten auffassen.

2. Im folgenden gehen wir von der Differenz zwischen zentripetalen und zentrifugalen Sandwiches aus (vgl. Toth 2026a):

zentripetale Sandwiches

$$R = ((\square, \square, \square) \rightarrow (\blacksquare, \blacksquare, \blacksquare) \leftarrow (\square, \square, \square))$$

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zentrifugale Sandwiches

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und stellen die 12 nicht-eigenrealen und eigenrealen Sandwichthematizationen im vollständigen semiotischen 27er-System mit Hilfe der ternär-triadischen Semiotik (vgl. Toth 2026b) dar.

1. Sandwichthematization

$$3.1 \quad 2.2 \quad 1.1 \quad \times \quad 1.1 \quad 2.2 \quad 1.3 \quad (1.1 \rightarrow 2.2 \leftarrow 1.3)$$

zentripetale Sandwiches

$$R = ((1, 1, \square) \rightarrow (1, 3, \square) \leftarrow (2, 2, \square))$$

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## 2. Sandwichthematisation

$$3.1 \quad 2.2 \quad 1.3 \quad \times \quad 3.1 \quad 2.2 \quad 1.3 \quad (3.1 \rightarrow 2.2 \leftarrow 1.3)$$

### zentripetale Sandwiches

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## 3. Sandwichthematisation

$$3.1 \quad 2.3 \quad 1.1 \quad \times \quad 1.1 \quad 3.2 \quad 1.3 \quad (1.1 \rightarrow 3.2 \leftarrow 1.3)$$

### zentripetale Sandwiches

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#### 4. Sandwichthematisation

$$3.1 \quad 2.3 \quad 1.2 \quad \times \quad 2.1 \quad 3.2 \quad 1.3 \quad (2.1 \rightarrow 3.2 \leftarrow 1.3)$$

zentripetale Sandwiches

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## 5. Sandwichthematisation

3.2 2.1 1.2 × 2.1 1.2 2.3 (2.1 → 1.2 ← 2.3)

### zentripetale Sandwiches

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## 6. Sandwichthematisation

3.2 2.1 1.3 × 3.1 1.2 2.3 (3.1 → 1.2 ← 2.3)

### zentripetale Sandwiches

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### 7. Sandwichthematisation

$$3.2 \quad 2.3 \quad 1.1 \quad \times \quad 1.1 \quad 3.2 \quad 2.3 \quad (1.1 \rightarrow 3.2 \leftarrow 2.3)$$

#### zentripetale Sandwiches

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### 8. Sandwichthematisation

$$3.2 \quad 2.3 \quad 1.2 \quad \times \quad 2.1 \quad 3.2 \quad 2.3 \quad (2.1 \rightarrow 3.2 \leftarrow 2.3)$$

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## 9. Sandwichthematisation

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## 10. Sandwichthematisierung

3.3 2.1 1.3 × 3.1 1.2 3.3 (3.1 → 1.2 ← 3.3)

zentripetale Sandwiches

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## 11. Sandwichthematisierung

3.3 2.2 1.1 × 1.1 2.2 3.3 (1.1 → 2.2 ← 3.3)

zentripetale Sandwiches

$$R = ((1, 1, \square) \rightarrow (2, 2, \square) \leftarrow (3, 3, \square))$$

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## 12. Sandwichthematization

$$3.3 \quad 2.2 \quad 1.3 \quad \times \quad 3.1 \quad 2.2 \quad 3.3 \quad (3.1 \rightarrow 2.2 \leftarrow 3.3)$$

### zentripetale Sandwiches

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